



Explanatory machine learning for sequential human teaching

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Which task would you first select to teach children?

Arrange fruits of different weights by merge sort



Increasing weights from left to right

Merge



Increasing weights from left to right

Sort

Using machine learned output for **knowledge transfer**

Ultra-Strong Machine Learning (USML) [Michie, 1988]

- ML outputs in **symbolic** representation
- The output can be **taught** to humans whose **performance can increase** to a level beyond learning from training examples

USML and Inductive Logic Programming (ILP)

Background BK: { father(john,susan). parent(susan,sam). }

Examples E+: { grandfather(john,sam). }

Hypothesis H: { grandfather(X,Y) :- father(X,Z), parent(Z,Y). }

BK U H should cover E+ and none of E-

*The world's **1st demonstration** of USML is in ILP [Muggleton et al., 2018]*

Are logic programs from ML suitable for knowledge transfer?

Minimal guidance **curriculum**



No guidance

Full guidance

- Learning merge sort via ILP
- Teaching merge sort
- Comprehension assessment
- Empirical results
- Remarks

ILP: Meta-Interpretive Learning

Background BK: { father(john,susan). parent(susan,sam). }

Example E+: { grandfather(john,sam). }

Higher-order Meta-rule M: { **P(X,Y) :- Q(X,Z), R(Z,Y).** }

Hypothesis H: { grandfather(X,Y) :- father(X,Z), parent(Z,Y). }

BK U H should cover E+ and none of E-
and **instantiate M**

Can learn *recursive logic programs* and invent *new predicates*!

A variant of **bottom-up** merge sort [Goldstine & Neumann, 1963]

```
merger (A,B) :-parse_exprs (A,C) ,merger_1 (C,B) .  
  
merger_1 (A,B) :- compare_nums (A,C) ,merger_1 (C,B) .  
  
merger_1 (A,B) :-compare_nums (A,C) ,drop_bag_remaining (C,B) .  
  
sorter (A,B) :-merger (A,C) , sorter (C,B) .  
  
sorter (A,B) :-recycle_memory (A,C) , sorter (C,B) .  
  
sorter (A,B) :-single_expr (A,C) , single_expr (C,B) .
```

Produced by a Meta-Interpretive
Learning system *Metagol*

Input:

[4, 6, 5, 2, 3, 1]

After Iteration 1

[4 < 6, 2 < 5, 1 < 3]

After Iteration 2

[2 < 4 < 5 < 6, 1 < 3]

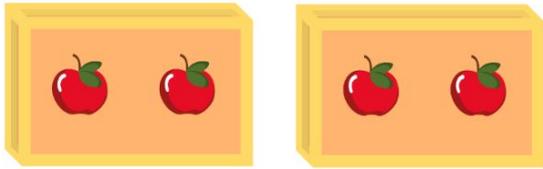
After Iteration 3

[1 < 2 < 3 < 4 < 5 < 6]

- Learning merge sort via ILP
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A case study: teach **Merge Sort** to human novices

Incremental



Increasing weights from left to right

Merge

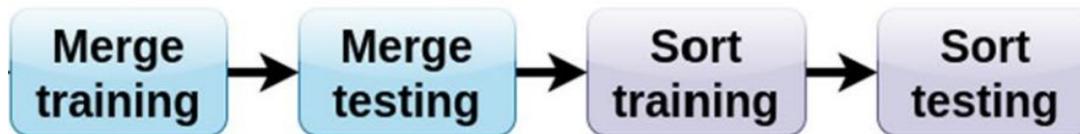


Increasing weights from left to right

Sort

2x2 Experimental design

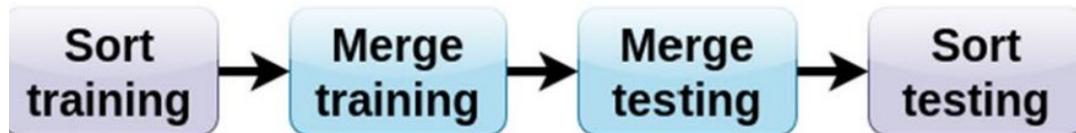
(a) Merge-then-sort



<1> With explanations

<2> Only examples

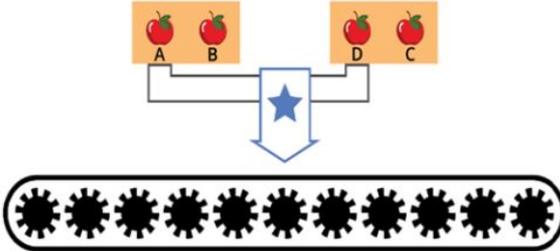
(b) Sort-then-merge



Learning to merge via **multiple-choice** questions



Compare



1. Use the scale on the left to COMPARE weights of TWO fruits by entering the alphabetic CAPITAL labels

2. In EACH ORANGE box, fruits are arranged in INCREASING weights from LEFT to RIGHT

3. Fruits on the CONVEYOR BELT are arranged in INCREASING weights from LEFT to RIGHT

You have 90 SECS to SUBMIT!

Please SELECT the CONVEYOR BELT that has the correct fruit(s) on YELLOW position(s):

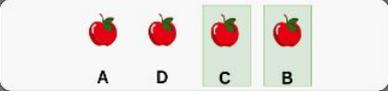
   

Submit

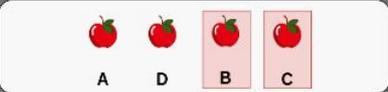
   

Submit

Explanations: why is/isn't an action optimal?

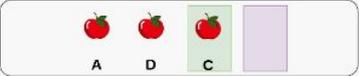
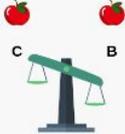


This answer is CORRECT!

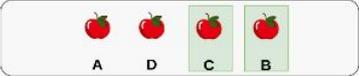


SELECTED >>>
This answer is WRONG!

Item C is lighter than item B; append item C

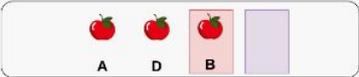
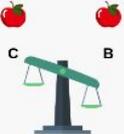


Append remaining item(s): B



The correct action sequence

Item C is lighter than item B so item C should be appended



A revision

Learning to sort through **explorations**



Compare



1. Use the scale on the left to **COMPARE** weights of **TWO** fruits by entering the alphabetic **CAPITAL** labels
2. You are given a **PILE** of fruits that is most likely **UNORDERED** and you can move fruits freely on the **MONITOR** in the middle to help you arrange fruits
3. The **PURPLE DIAMOND** puts fruits from the **PILE** into the **SHIPPING CRATE** in **INCREASING** weights from **LEFT** to **RIGHT**
4. You can see the **NUMBER OF COMPARISONS** BOB uses as a reference and you have **300 SECS** to **SUBMIT!**

Put fruits on the **SHIPPING CRATE** by entering their labels one by one into the following boxes with **WEIGHT INCREASING** from **LEFT** to **RIGHT**

BOB uses 8 comparisons
You have used: 0

Submit

- Learning merge sort via ILP
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Ultra-strong ML -> human behavioural change

Explanatory effect =

machine-aided task performance - self-learning task performance

Machine-aided: with explanations (e.g. generated from LP)

Self-learning: with only training examples

Performance: predictive accuracy on unseen tests

Evaluating human sorting performance

Spearman rank correlation coefficient [Spearman, 1904]:

Non-parametric test of the **monotonicity** between the **rank values** of two variables **X** , **Y**

$$\frac{\text{cov}(R(X), R(Y))}{\sigma_{R(X)} \sigma_{R(Y)}}$$

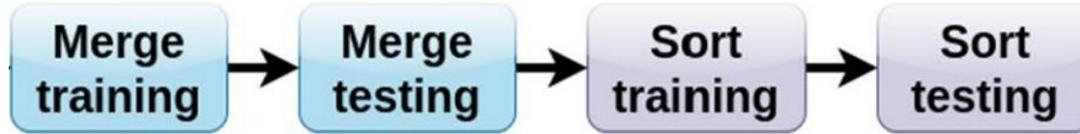
E.g. **X** : [1, 2, 3, 4, 5, 6]

$Y1$: [4, 6, 5, 2, 3, 1]

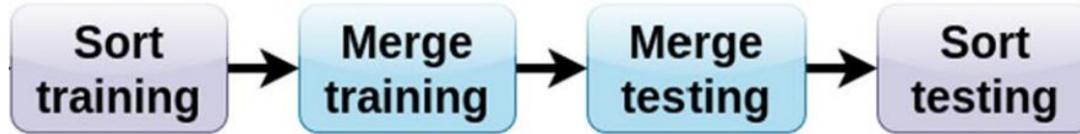
$Y2$: [1, 2, 6, 3, 4, 5]

$$\rho(\mathbf{X}, \mathbf{Y1}) < \rho(\mathbf{X}, \mathbf{Y2})$$

Comparing between different curriculum order



(a)



(b)

Effect of curriculum on task T =

Performance of T in (a) - Performance of T in (b)

Can we identify human **sorting strategy**?

Sequence [4, 6, 5, 2, 3, 1]

Human trace:

[(6, 4), (5, 2), (3, 1), (4, 2), (5, 4), (6, 5), (2, 1), (3, 2), (4, 3)]

Machine trace (24 algorithms, 6 categories):

[(4, 6), (5, 2), (2, 4), (4, 5), (5, 6), (3, 1), (1, 2), (2, 3), (3, 4)]

There are 21 possible pairs (symmetric pairs are considered identical).

An example of **trace-based** evaluation

Step 1: Identify common/different pairs via χ^2

	Not in human trace	In human trace
Not in machine trace	13	1
In machine trace	1	10

(Added 1s to avoid zero cells)

$$\chi^2 = 14.3 \text{ with } p < .001$$

Step 2: Rank algorithms via spearman rank correlation

Spearman rank correlation $\rho = .9$ and $p < .001$

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Cognitive window for a machine-learned logic program P

Axiom 1: Hypothesis space to necessarily learn P must be small

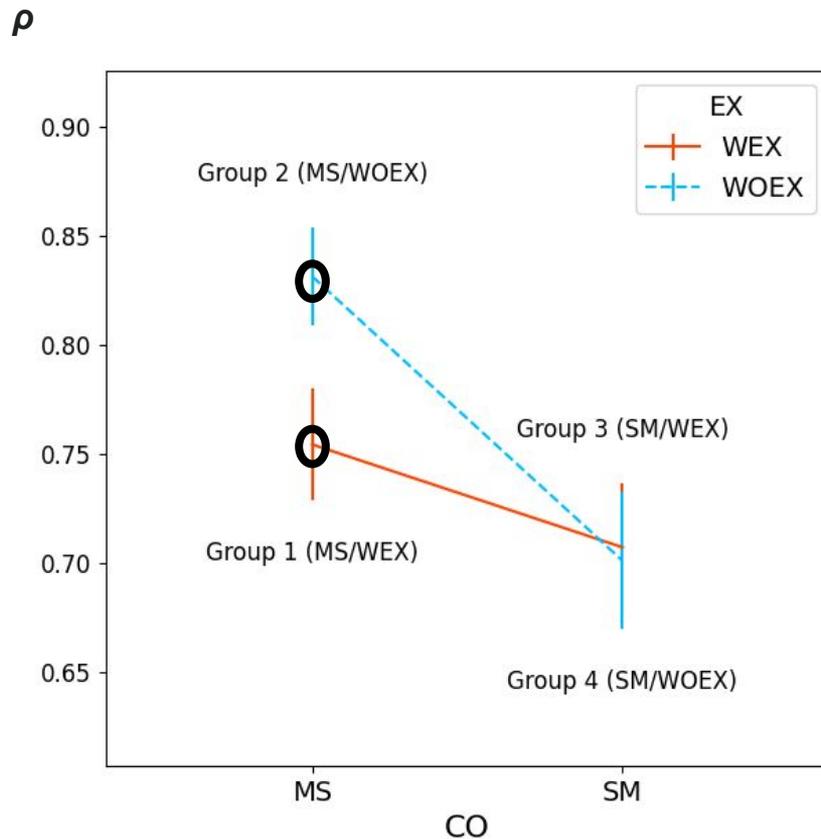
Humans have limited search ability in the hypothesis space

Axiom 2: P has “shortcuts” to reduce grounding cost

Humans have limited capacity for mental computations

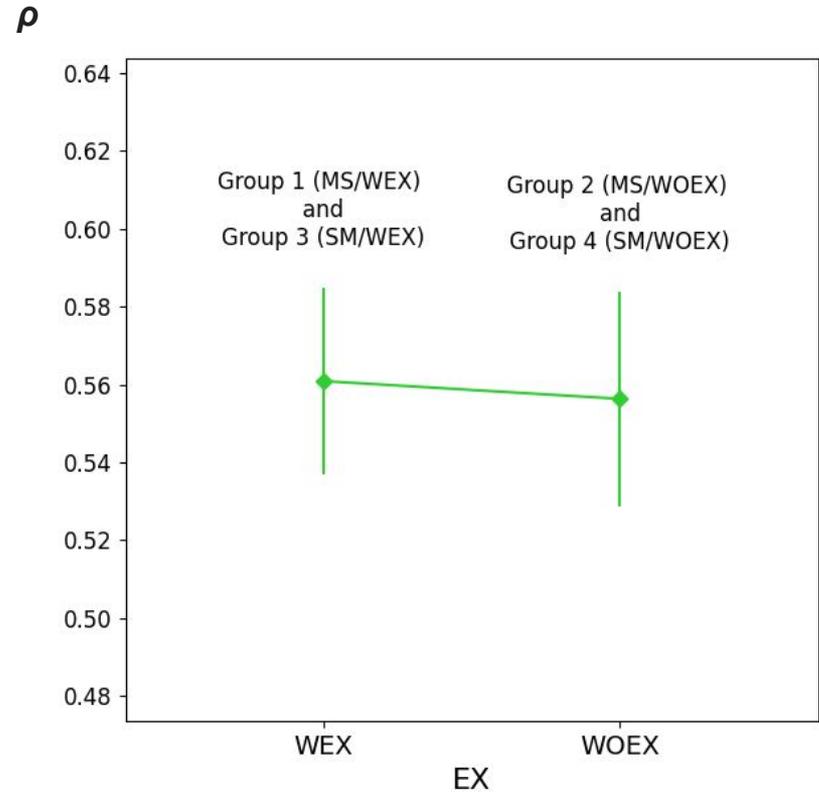
Merge-then-sort learning **reduces total hypothesis space size**

Improved performance
(**supports Axiom 1**)



Explanations contain no “shortcuts” to merging

No performance differences
(supports Axiom 2)



Effects of **Incremental** learning with **explanations**

	Algorithm	Is adaptation	Is performance
Group	adapted	significant	improvement significant
Group 1 (MS/WEX)	QS	✓	✓
Group 2 (MS/WOEX)	MS	✓	X
Group 3 (SM/WEX)	DS	X	✓
Group 4 (SM/WOEX)	IS	✓	✓

Increased application of **quick sort like** algorithms

=> **higher performance** than other approaches

Impact of explanations on **performance**

	Algorithm	Is adaptation	Is performance
Group	adapted	significant	improvement significant
Group 1 (MS/WEX)	QS	✓	✓
Group 2 (MS/WOEX)	MS	✓	X
Group 3 (SM/WEX)	DS	X	✓
Group 4 (SM/WOEX)	IS	✓	✓

Explanations **contextualise the binary selection** concept

(quick sort, dictionary sort)

Impact of incremental curriculum on **strategy adaptation**

	Algorithm	Is adaptation	Is performance
Group	adapted	significant	improvement significant
Group 1 (MS/WEX)	QS	✓	✓
Group 2 (MS/WOEX)	MS	✓	X
Group 3 (SM/WEX)	DS	X	✓
Group 4 (SM/WOEX)	IS	✓	✓

Incremental curriculum helps **reduce hypothesis size** for learning

divide-and-conquer algorithms (quick sort, merge sort)

- Learning merge sort via ILP
- Teaching merge sort
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Learning merge sort is a **challenging** task



Concluding remarks

While we took a **minimalist** approach,

- teaching logic programs can lead to **remarkable re-discoveries**
- incremental learning and explanations had a **USML potential**
- results supported the **cognitive window**

Future work

- Beyond **ILP** and **noise-free** framework
- Two-way learning via **behavioural cloning**
- Curricula and optimisations for **human discovery**

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